

Second-Order Effects

When flexure is introduced into an axially loaded member from the axial force acting through the sidesway of a frame and curvature of a member, this is referred to as a second-order effect. The analysis of the structure must be modified to capture the impact of these effects, as they will not be realized in a first-order design model of initially plumb frames and straight members. The primary effects to be considered are $P-\Delta$ moments, associated with the sidesway of the structure, and $P-\delta$ moments, associated with the curvature of each individual member as it deflects and deforms.

The moments generated by these effects can be captured in the analysis in several ways, and any method that a designer chooses to analyze a structure that captures each of the possible effects is acceptable. Therefore, it is equally permissible to analyze a structure by a direct, rigorous second-order analysis, or to use an approximate method of second-order analysis, such as the one presented in Section C2.1b.

In the former case, the frame and member deformations are tracked directly within the analysis software as a part of the analysis. In the latter case, a first-order analysis is made and the resulting forces and moments are amplified using the variables B

Each of these effects is considered in all three stability design methods presented in the AISC Specification (the Effective Length Method in Section C2.2a, the First-Order Analysis Method in Section C2.2b, and the Direct Analysis Method in Appendix 5). The Direct Analysis Method does not use deformation amplification. It eliminates the need to calculate K -factors in design. The K -factor, a long-standing feature of structural frame design, is well accepted as a means to implicitly capture many of these effects, in spite of its many limitations and underlying assumptions that are rarely satisfied in real structures.

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B_1 and B_2 from the AISC

Stability Analysis: It's not as Hard as You Think

The Direct Analysis Method is a good choice for stability design—and with a little guidance, it can be a relatively simple process.

STABILITY IS FUNDAMENTAL TO DESIGN, YET IT CAN BE CHALLENGING TO understand, as many of the current provisions are new. The AISC Specification allows designers to use any method of stability analysis that considers each of the following:

- Second-order effects
- Flexural, shear, and axial deformations
- Component and connection deformations
- Member stiffness reduction due to residual stresses
- Geometric imperfections

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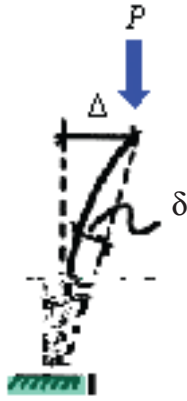


Figure 1. Basic model describing P - and P - δ effects for a single fixed-base column.

Deformation of the Structure

Engineers are generally familiar with methods of calculating the deflections of members under load. While the structure can be analyzed conventionally for the deflections of individual members, it is important to be sure that these deflections are captured in a second-order analysis of the frame. As stated previously, it is equally permissible to analyze a structure by a direct, rigorous second-order analysis, or to use an approximate method of second-order analysis, such as the one presented in *AISC C* Section C2.1b. It also is important to consider the effect of connection and panel-zone deformations in the analysis.

Residual Stresses

Residual stresses are introduced into structural shapes as a result of the pro-

duction process. Residual stresses include stresses due to temperature, as some elements of the hot rolled cross-section will cool faster than others, and also due to the effects of straightening that must be done to meet ASTM A6 tolerances. Areas with residual stress will yield prior to the overall yielding of the section, causing the column to lose some of its stiffness before reaching its theoretical buckling strength. The effects of residual stresses on member strength are accounted for in the column equations. However, the loss of stiffness due to residual stresses also will increase the frame and member deformations. This is accounted for in the Direct Analysis Method by using a reduced stiffness for all members in the analysis: multiplying the axial stiffness, EA , of all members by 0.8 and multiplying the flexural stiffness, EI , of all members by 0.8τ , where τ is the column stiffness reduction factor.

Geometric Imperfections

Geometric imperfections are inherent in all structures, and limits on these are found in the *AISC C* (plumbness of frames) and the *ASTM* standards for structural shapes (straightness of members). Frame out-of-plumbness is modeled directly in the Direct Analysis Method using notional loads acting laterally at each floor (alternatively, this can be done by direct modeling of the out-of-plumb frame geometry, if it is known).

A notional load is an equivalent lateral load of appropriate magnitude such that it

will generate a story shear in the structural model equivalent to the effect of the axial loads in a story acting in the deformed position, as illustrated in Figure 2. According to the *AISC C*, the permissible tolerance on out-of-plumbness of any individual column is no larger than $L/500$, and the notional load is specified to generate a story shear corresponding to this amount of out-of-plumbness. A horizontal notional load of 0.002 times the story gravity load in the horizontal direction is applied, with the 0.002 coefficient being equal to $1/500$ —the erection tolerance permitted by the *C*.

Leaning Columns

In any stability analysis, it is necessary to capture the destabilizing effects of columns that rely on the lateral frame for stability but are not a part of the lateral frame. These columns with pinned ends are commonly referred to as “leaning columns.” When modeling the frame, leaning-column effects can be captured either by developing a complete 3D model of the frame or by assigning a single equivalent leaning column carrying the summation of all of the gravity loads on all of the leaning columns in the structure, as a pin-connected part of a 2D frame. An example of how this might be modeled in a 2D analysis is shown in Figure 3.

Step-by-Step Analysis

Now that you know the basics, here is a simple step-by-step process to guide you as you use the Direct Analysis Method:

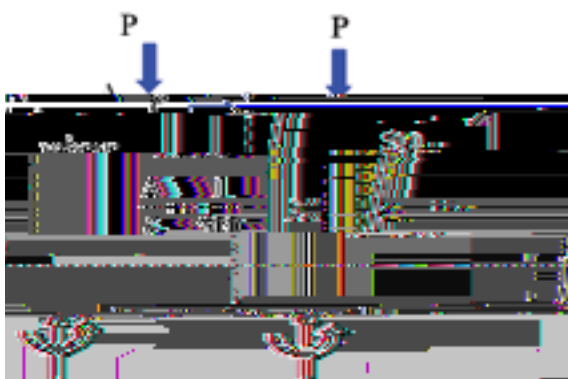


Figure 2. Equivalent loading using notional loads to represent the effect of geometric imperfections on a column.

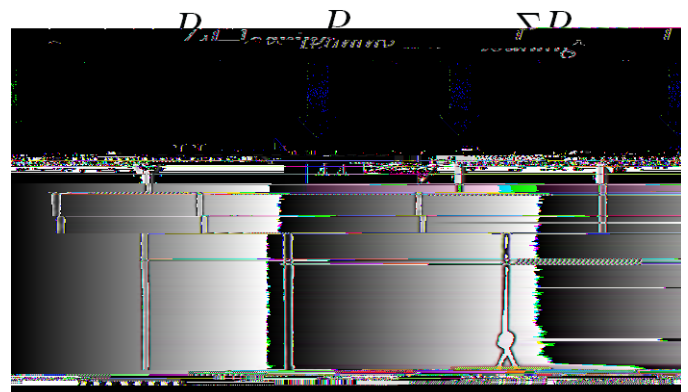


Figure 3. 2D frame model that captures leaning column effects.

1. Create a model of the lateral frame being analyzed, including the leaning columns.
- 2.

